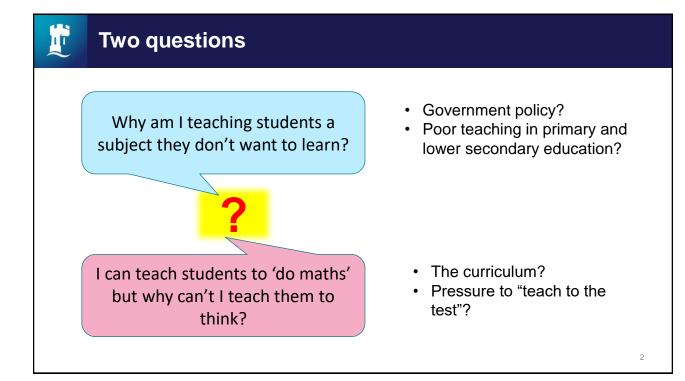
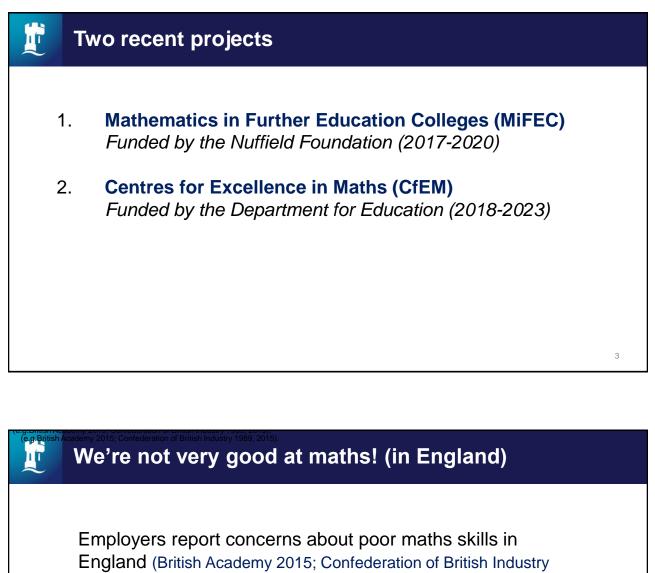


University of Nottingham

Opening up the black box: the challenges of teaching mathematics within vocational education

Dr Diane Dalby September 2022

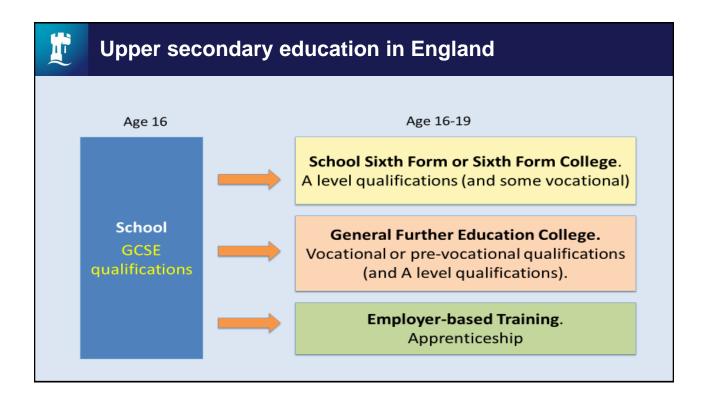




1989, 2015).

National surveys report low levels of numeracy skills (Moser 1999; BIS 2011; National Numeracy 2014).

International comparisons highlight England's relatively poor numeracy skills (Wheater et al. 2013; Kankaraš et al. 2016).



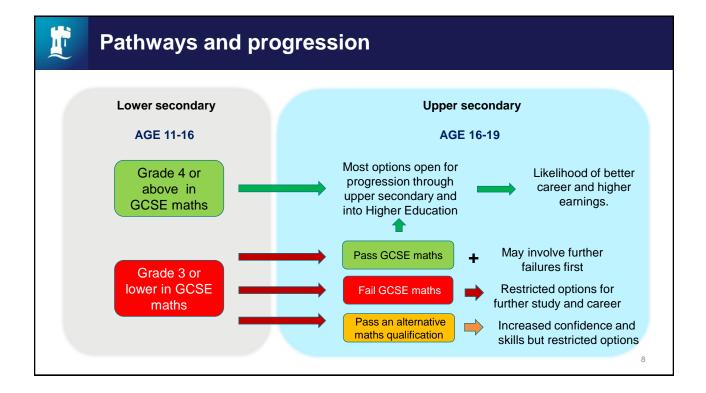


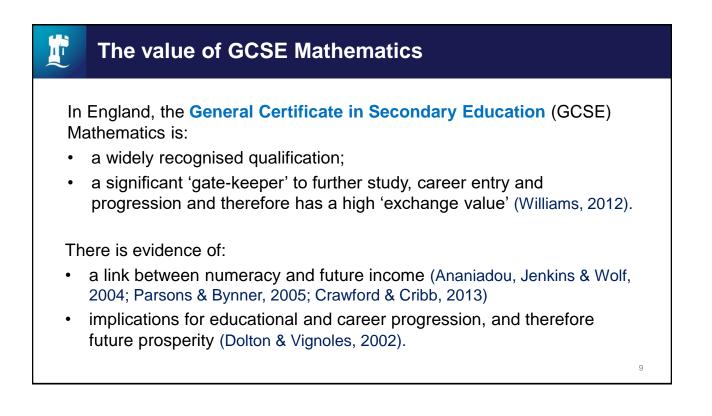
Post-16 mathematics policy in England

Since September 2014, those who fail to reach a specified minimum standard in GCSE mathematics (grade 4) by age 16 have been required to **continue studying** the subject in post-16 education (upper secondary), with the aim of **retaking** the examination and **achieving grade 4**.

Those with lowest GCSE grades at age 16 (grades 1 and 2) may take a **Functional Skills qualification** first as a 'stepping stone'.

The majority of those required to retake mathematics under this policy follow **vocational pathways** post-16, mostly in Further Education colleges.



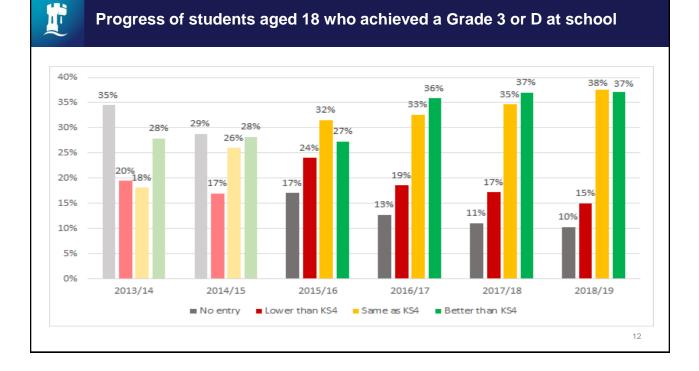


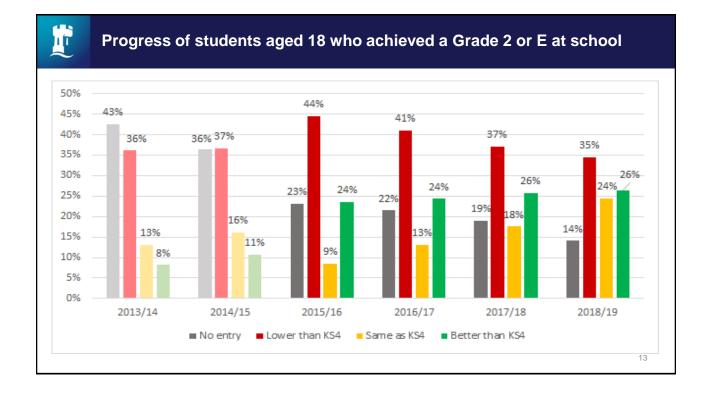


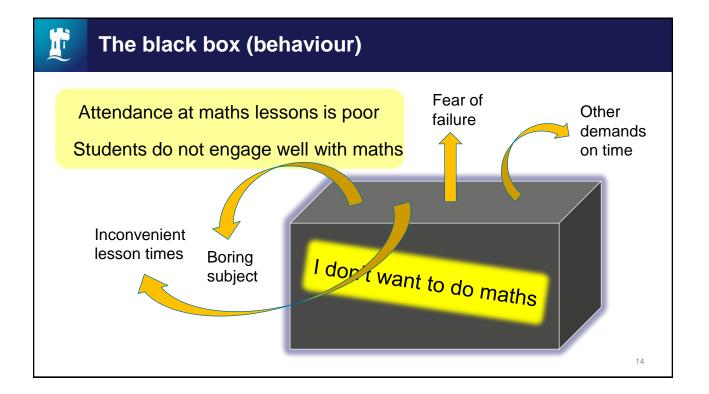
Mathematics in Further Education Colleges project

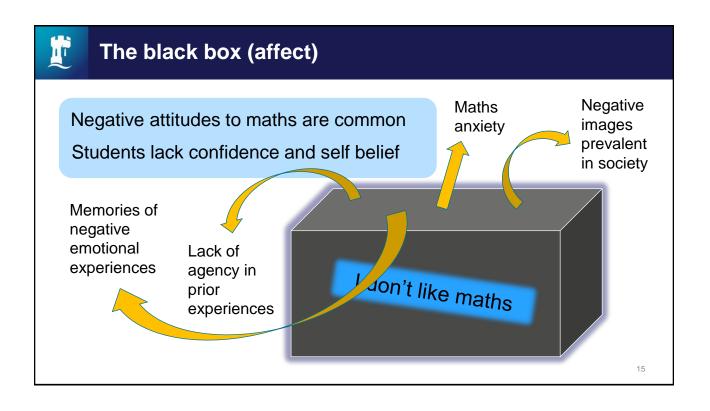
The MiFEC project aimed to produce evidence-based advice for policymakers, college managers and practitioners on how to improve mathematics education in England's General Further Education colleges. The final report and four interim reports can be found at http://www.nottingham.ac.uk/research/groups/crme/projects/mifec/index.aspx

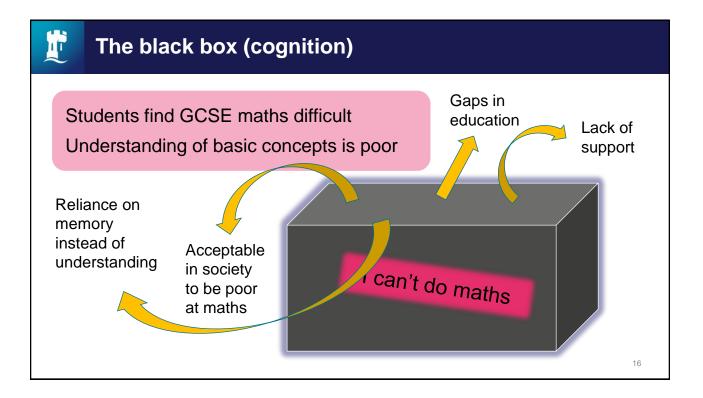
- 1. National policy trajectory analysis and literature review.
- 2. Analysis of student progression over time (using national datasets).
- Case studies of 32 colleges (238 staff interviews, 62 student focus groups).
- 4. Mathematics workforce survey.











Transition to vocational education



- · Working with real clients
- Working to professional standards
- Working within health and safety guidelines
- Learning skills relevant to personal aspirations and intended employment destinations

Changing identities with work-related values

Negotiating the vocational-academic divide



- Academic subject
- Teacher-focussed
 approach
- Formal social structure

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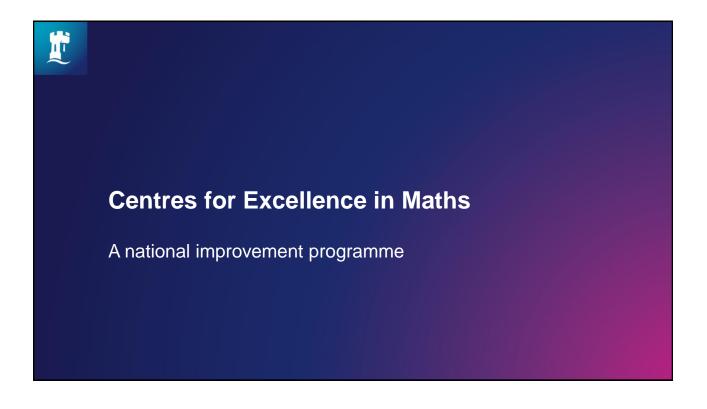
The connected approach

Classroom culture

- A culture that reflects vocational values;
- A social structure with **greater agency** for students than usually found in a traditional school mathematics classroom;
- Positive teacher-student **relationships** in which the teachers facilitates learning;
- A 'safe' environment for students.

Pedagogy

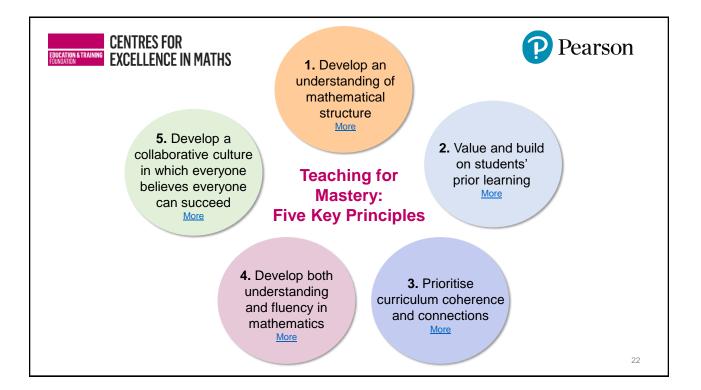
- Understanding of *signature* pedagogies;
- Appropriate use of vocational contexts (to highlight relevance or develop conceptual understanding);
- Workplace examples that demonstrate use-value;
- Synchronisation of maths and vocational schemes of work.



Centres for Excellence in Maths

Centres for Excellence in Maths (CfEM) is a five-year programme aimed at delivering sustained improvements in maths outcomes for 16–19-year-olds, up to Level 2 (GCSE level), in post-16 settings. The programme is exploring what works for teachers and students, embedding related CPD and good practice, and building networks of maths professionals in colleges. It involves 21 FE colleges, each with a network of partner colleges.

- Teaching for Mastery in FE project (Randomised Control Trials)
- Whole College Approach research project



Dialogue in the classroom

A co-construction of knowledge by 'doing things with others' (Watkins, 2005).

The form and purpose of student dialogue is shaped by the nature of the **teacher talk** that precedes or accompanies it (Alexander, 2018).

Object-level or meta-level **changes in classroom discourse** may occur (Sfard 2015).

	Activity	Time (min)	Description/Prompt
	Introduction	5	Introduce the context of buying a baguette to share for lunch. Discuss how the baguette can be shared and remind students of the language of fractions and ratios.
	Explore 1	10	Ask the students to work in pairs, matching fraction cards to ratio descriptions of different ways the baguette could be shared.
Lesson 2: Ratio and fractions	Explore 2	15	When students are a substantial way through matching ratios and fractions give them some diagram cards to place in the column between the ratio and fraction columns.
	Explore 3	15	Once students have completed the ratio-diagram-fraction matches give them a set of description cards to place along the edge of the grid.
	Discuss	15	Discuss what completing the 'Diagram' column revealed about the relationship between fractions and ratios. Discuss how students adjusted their cards after being given the diagram cards.
	Review	20	With the students, explore a common misconception and discuss how fractions and ratios are linked. Describe part—whole and part—part relationships.
	Practice question	10	Ask students to answer an exam question and after a few minutes discuss their thinking.

Principles of dialogic teaching

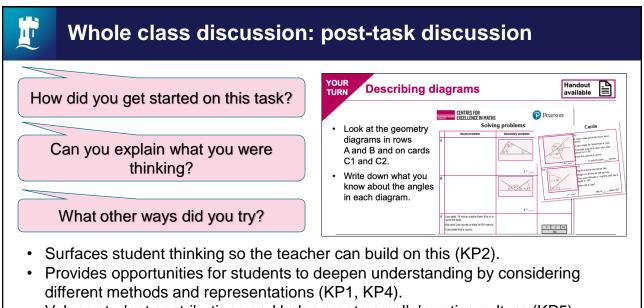
Collective - the classroom is a site of joint learning and enquiry. **Reciprocal** - participants listen to each other, share ideas and consider alternative viewpoints.

Supportive - participants feel able to express ideas freely, without risk of embarrassment over 'wrong' answers, and they help each other to reach common understandings.

Cumulative - participants build on their own and each other's contributions and chain them into coherent lines of thinking and understanding.

Purposeful - classroom talk, though open and dialogic, is structured with specific learning goals in view. (Alexander 2018)

Whole class discussion: initial task (Case study A) Making walls out of blocks What ideas did you have about this question? Em Who had a different approach? Twice as Finch ong as Em's wall Can anyone explain how that 3 times as What are possible long as Em's works? lengths for the 3 walls? Exposes prior learning so teacher can build on this (KP2). Demonstrates that student contributions are valued and helps create a collaborative culture in which everyone believes everyone can succeed (KP5). Collective – Reciprocal – Supportive – Cumulative 26



• Values student contributions and helps create a collaborative culture (KP5).

Collective – Reciprocal – Supportive

Approaches use	Approaches used						
 Case Study A Invites students to offer ideas and explanations of their thinking. Follows with questions to probe further into students' thinking. Asks students for alternative approaches and methods. Invites students to help each other with 	 their methods. Sometimes asks for more explanation. Offers own explanations when a student seems stuck. 	 Case study C Asks students for the answers. Sometimes asks students to explain their methods. Rarely asks about any alternative approaches or ideas. Almost always ends by explaining a method themselves. 					

Creating and shaping dialogic spaces

Dialogue about mathematics was shaped by **sequencing** different types of questioning to expand and narrow discussions according to students' responses and needs. Teachers used a combination of:

- Open questions about students' ideas;
- Exploratory questions to follow up on students' responses and probe more deeply into their thinking;
- Invitations to offer further explanation and alternative ideas;
- Requests to help explain ideas proposed by other students or build on other students' ideas.

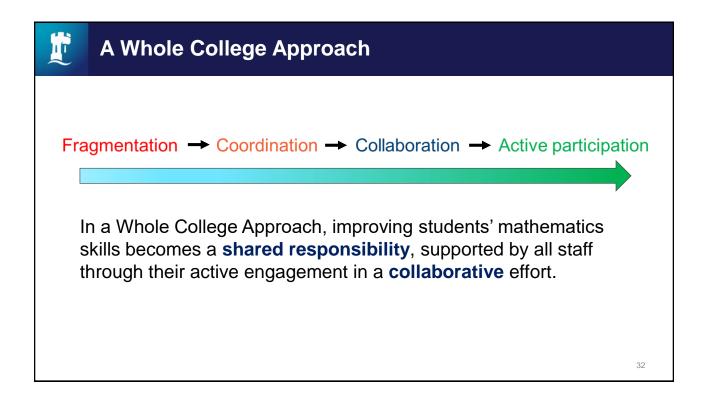


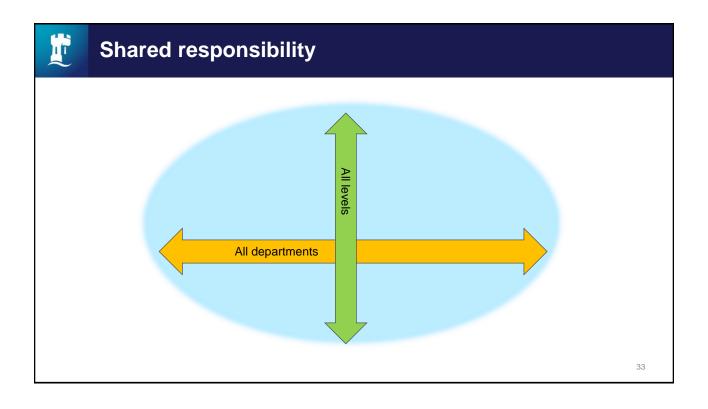
Background

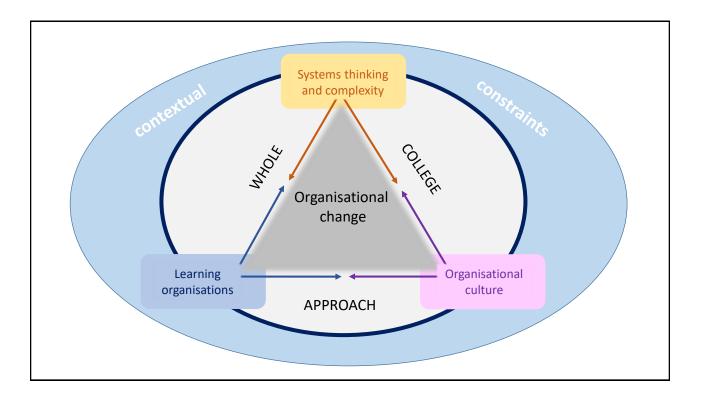
The Mathematics in Further Education Colleges project (MiFEC) evidenced broad agreement from a cross-section of staff in England's FE colleges that mathematics is **important** and that students with low attainment should be **improving their mathematics skills**.

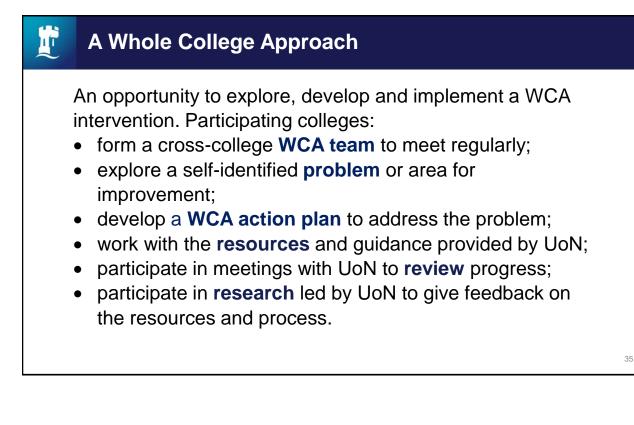
There was also evidence that:

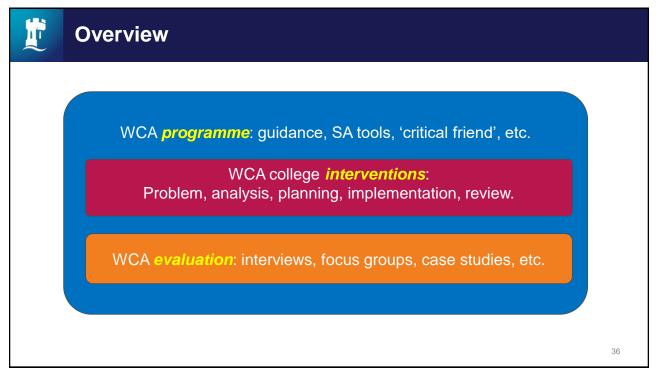
- students can receive inconsistent messages, explicitly and implicitly, about the need to engage with mathematics;
- combinations of strategic or operational approaches can produce variations in students' experiences and sometimes hinder their participation or progress.











		DISCOVERY PHASE			
SA1: context and readiness	SA2: c	SA2: climate		SA3: analysis	
 To develop: a shared understanding of college context; a shared understanding of organisational readiness to change; collaborative ways of work together within an openminded, inquiring and supportive culture. 	of th • bett pers muli ing • colla	velop: ared multidimensional ne college climate ; er understanding of dif pectives and their valu tidimensional analysis; aborative ways of work ther.	ferent • a detailed e in problem (u • Understan ing connection	Inderstanding of the and related issues; analysis of the Ising CHIME); ding of key elements, ns, affordances and s of systems and	
		CHIME framework			
CONTEXTUALISED HO	ustic erstanding o	INTERCONNECTED f context, climate and p	MULTIDIMENSIONAL	EVALUATIVE	
	into a collab	orative working group			
Development of WCA team					

Different perspectives

Through the Discovery Phase, colleges developed a better understanding of the problem and therefore a more appropriate action plan by meeting together and **sharing different perspectives** in open and honest conversations.

However, it should be noted that sometimes there was a need to **'broker' the discussion** with an independent chairperson, especially in situations where attitudes were deeply ingrained or there were initially strongly opposing views.

Addressing the problem

Most colleges found that the area or problem they eventually decided to tackle was **not the same** as the one they initially identified.

Colleges reported that by addressing one problem they often found the process they worked through also led to **improvements in other areas**.

Colleges reported that it has been important to consider both **systems and people** in their projects.

Common issues

Attendance at mathematics sessions

Increased **communication** about mathematics between maths and vocational teachers has improved communication about other matters such as student attendance and led to better mutual understanding.

Student engagement with mathematics

Colleges have used various approaches to make **curriculum connections** and develop **closer relationships** (e.g. using vocationally-relevant contexts, shared events, coordinated schemes of work, visits to each other's classrooms).

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There is more to say …

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